



RFI-mitigation using a PAF



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Outline

- Introduction
- Theoretical considerations
- Various “algorithms” and their effects
- Next steps
- Outlook

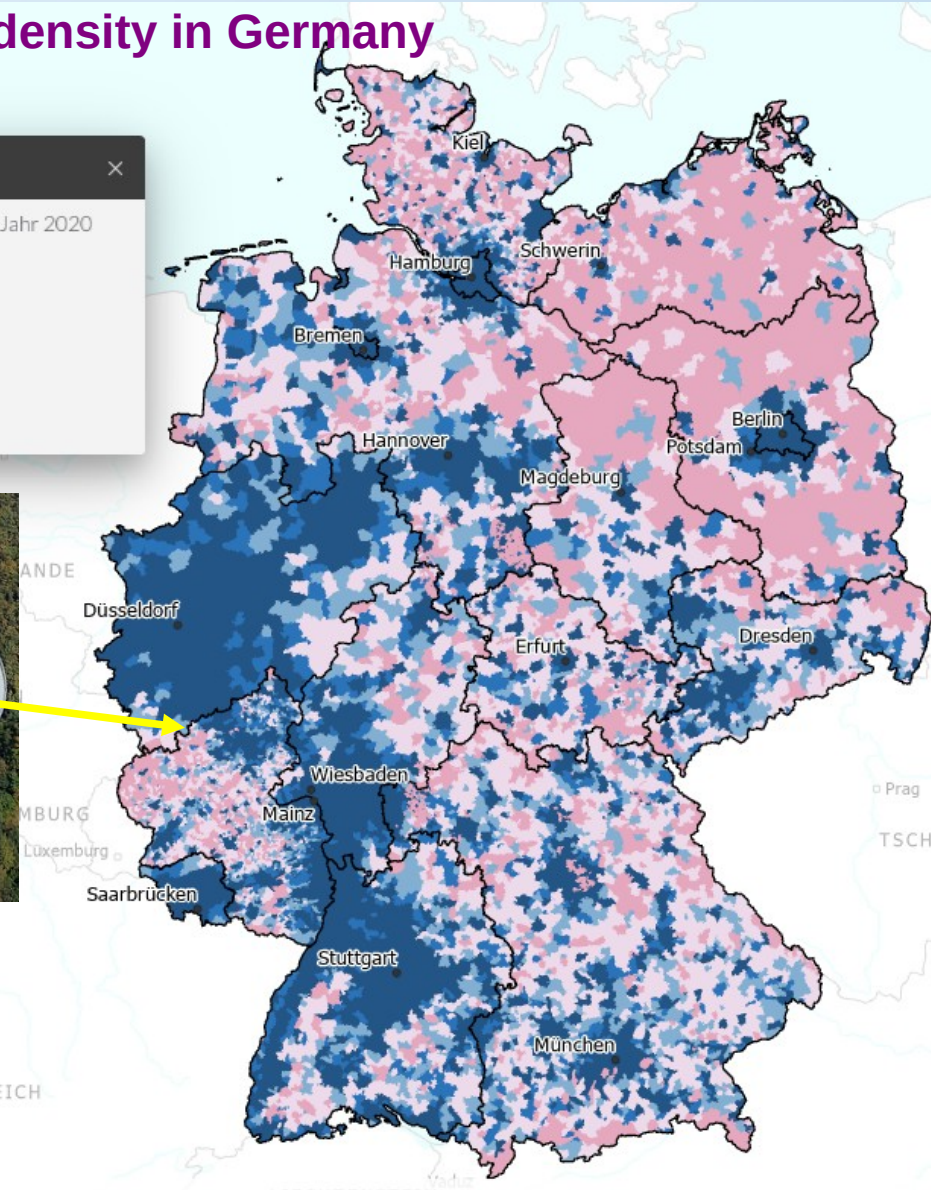
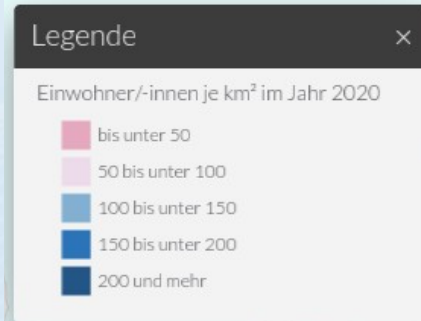




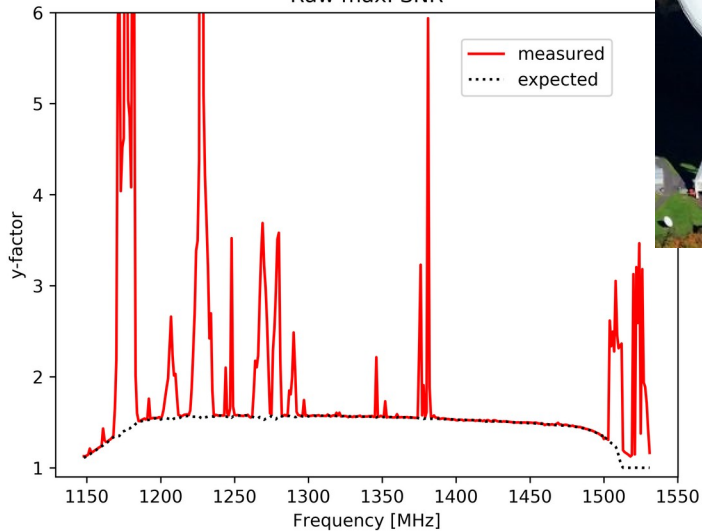
Introduction



Population density in Germany



Raw max. SNR



- The 100 m telescope is located close to one of the densest populated areas in central Europe
- Suffering from massive human made RFI
- Can a PAF help here?



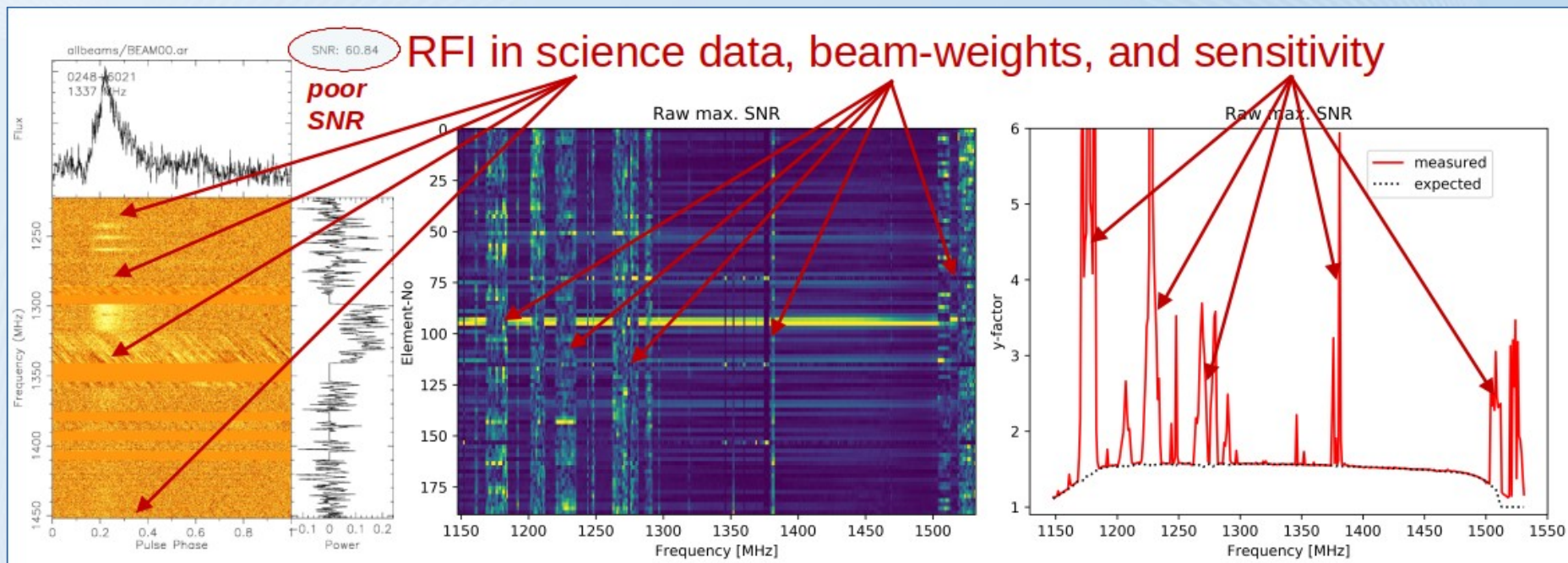
The situation in L-band



- we operate a CSIRO PAF at Effelsberg
 - we use it for testing, e.g. of the RFI environment
 - and of our algorithms
- we so far still hesitate with RFI during beam-forming
 - can be transferred to online RFI mitigation easily
 - ✓ e.g. by orthogonal projection



Top: CSIRO checkerboard PAF for the Effelsberg 100m telescope during its first installation (March 2017)





Theoretical considerations



- The signal to noise ratio of the formed beam can be written as

$$SNR = \frac{P_S}{P_N} = \frac{P_{on} - P_{off}}{P_{off}} = \frac{P_S}{P_N} - 1 = \frac{\vec{w}^H R_{on} \vec{w}}{\vec{w}^H R_{off} \vec{w}} - 1$$

- The sensitivity therefore results in

$$\frac{A_{eff}}{T_{sys}} = \frac{2k_B}{10^{-26} S} \left(\frac{\vec{w}^H R_{on} \vec{w}}{\vec{w}^H R_{off} \vec{w}} - 1 \right)$$

- Maximization of SNR+1 corresponds to solving the generalized eigenvalue problem

$$R_{on} \vec{w}_{mSNR} = \lambda_{max} R_{off} \vec{w}_{mSNR} \Leftrightarrow R_{off}^{-1} R_{on} \vec{w}_{mSNR} = \lambda_{max} \vec{w}_{mSNR}$$

- If we assume that the noise is

- statistically independent from the signal
- following a Gaussian (normal) distribution and is white

this is equal to solving $R_{on} \vec{u} = \kappa \vec{u}$

→ all solution vectors give the eigenvector decomposition of the ACM R_{on}

- ➔ the solution space includes beam-weights which correspond to RFI sources
- ➔ all solution vectors are mathematically orthogonal to each other
 - RFI can / will cause a loss of efficiency → calibration must be maintained !



RFI mitigation algorithms (1)



- Using the eigenvector decomposition of R_{on} and R_{off}
 - eigenvector decomposition of the array correlation matrix (ACM) give
 - ✓ steering vector towards source (ACM of an ON measurement only)
 - ✓ steering vector(s) towards RFI sources (ON and OFF measurement)
 - ✓ noise contributions
 - × “steering vectors” towards noise sources
(areas of different noise levels like termination on ground, or on sky)
 - the eigenvector decomposition allows for filtering if
 - ✓ eigenvalues of the RFI are higher than those belonging to noise or signal
 - ✓ problem is to distinguish between RFI, noise, and signal
 - hard filtering will/can remove good data
 - eigenvectors identified as RFI can not simply just be removed
 - ✓ this would lead to a lower rank of the matrix
 - not all mathematical operations would be allowed
 - ✓ therefore we just attenuate them (poor mans version)
 - (cleaner would be to calculate a sub-space orthogonal to RFI via projection)

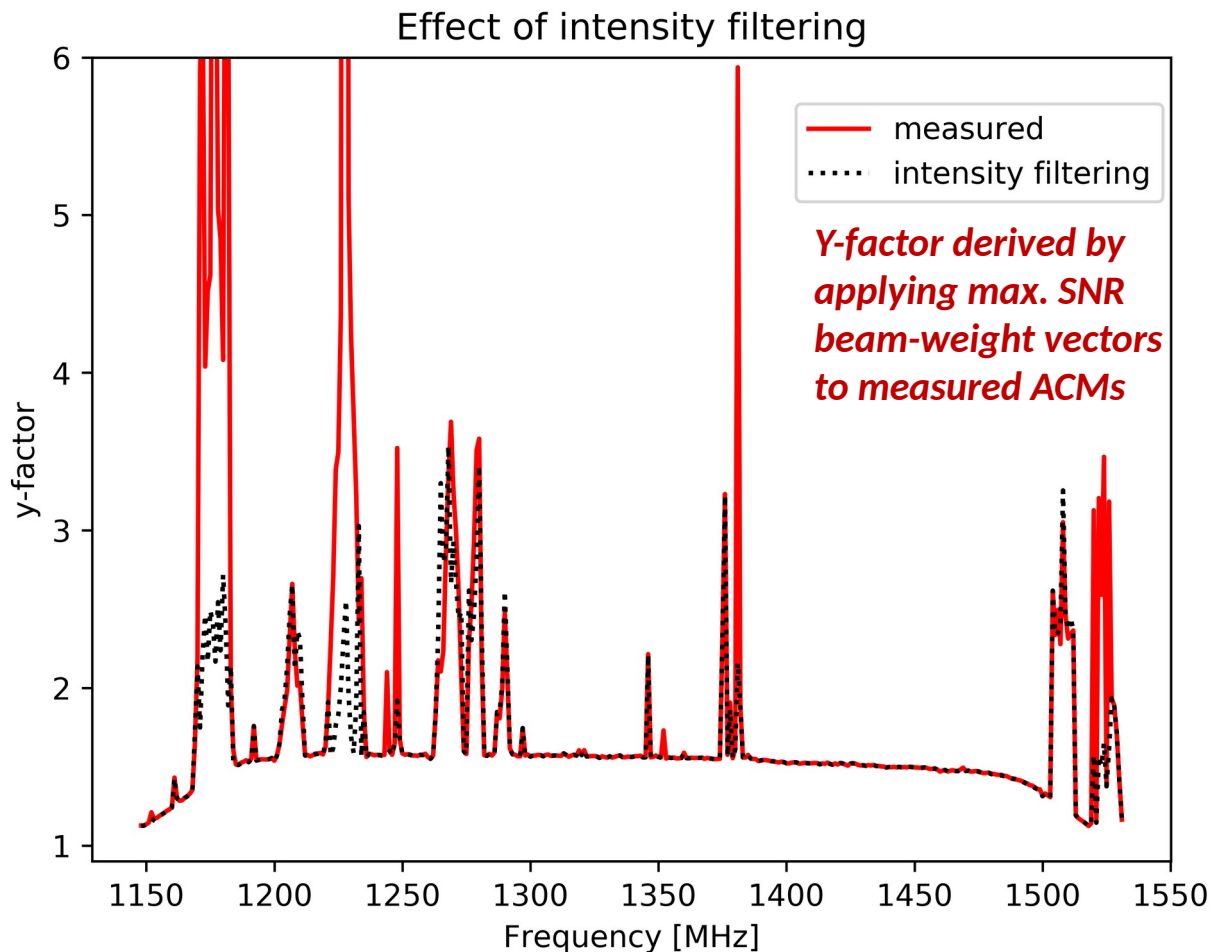
→ this is a filtering along the signal strength of the eigenvectors
→ can potentially remove the signal ...



RFI mitigation algorithms (1)



- Usi



- this is a filtering along the signal strength of the eigenvectors
- can potentially remove the signal ...



RFI mitigation algorithms (2)



- Selecting the “right” eigenvector from $\mathbf{R}_{\text{on}}\mathbf{R}_{\text{off}}^{-1}$
 - the highest eigenvalue not necessarily belongs to the astronomical signal source
 - ✓ can well be an RFI source!
 - how to identify the signal weight vector?
 - ✓ signal weight vectors must be nearly “parallel” to neighboring signal weight vector
 - ✓ frequency average of strongest eigenvector is a good starting point for a source steering vector
 - ✓ weight vectors towards RFI have a different “direction” than the ones towards source
 - ✗ can be identified using e.g. the dot-product with the neighboring source beam-weight vector
 - this will lead to problems if RFI and undisturbed source vector are not orthogonal
 - weight vectors can be interpolated over “empty” frequency areas
 - ✓ we are using an independent linear interpolation over real and imaginary part
- is used in science operation (for FRB search) since August 2020

→ this is a spacial filtering of the signals
→ works reliable on noisy ACMs (short integration time)
→ interpolation can cause problems



RFI mitigation algorithms (2)



- Selective

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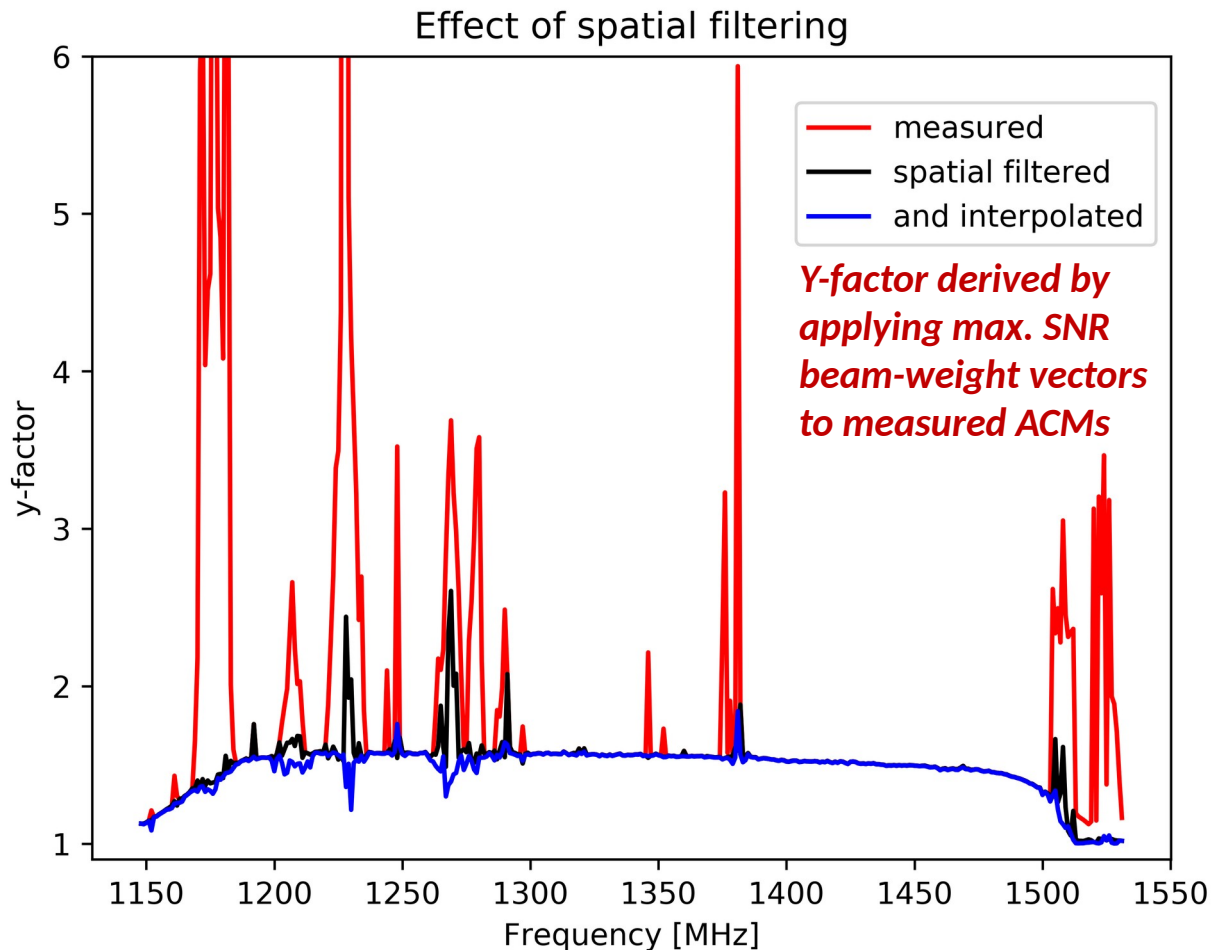
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- weigh



- is used i



→this is a spacial filtering of the signals

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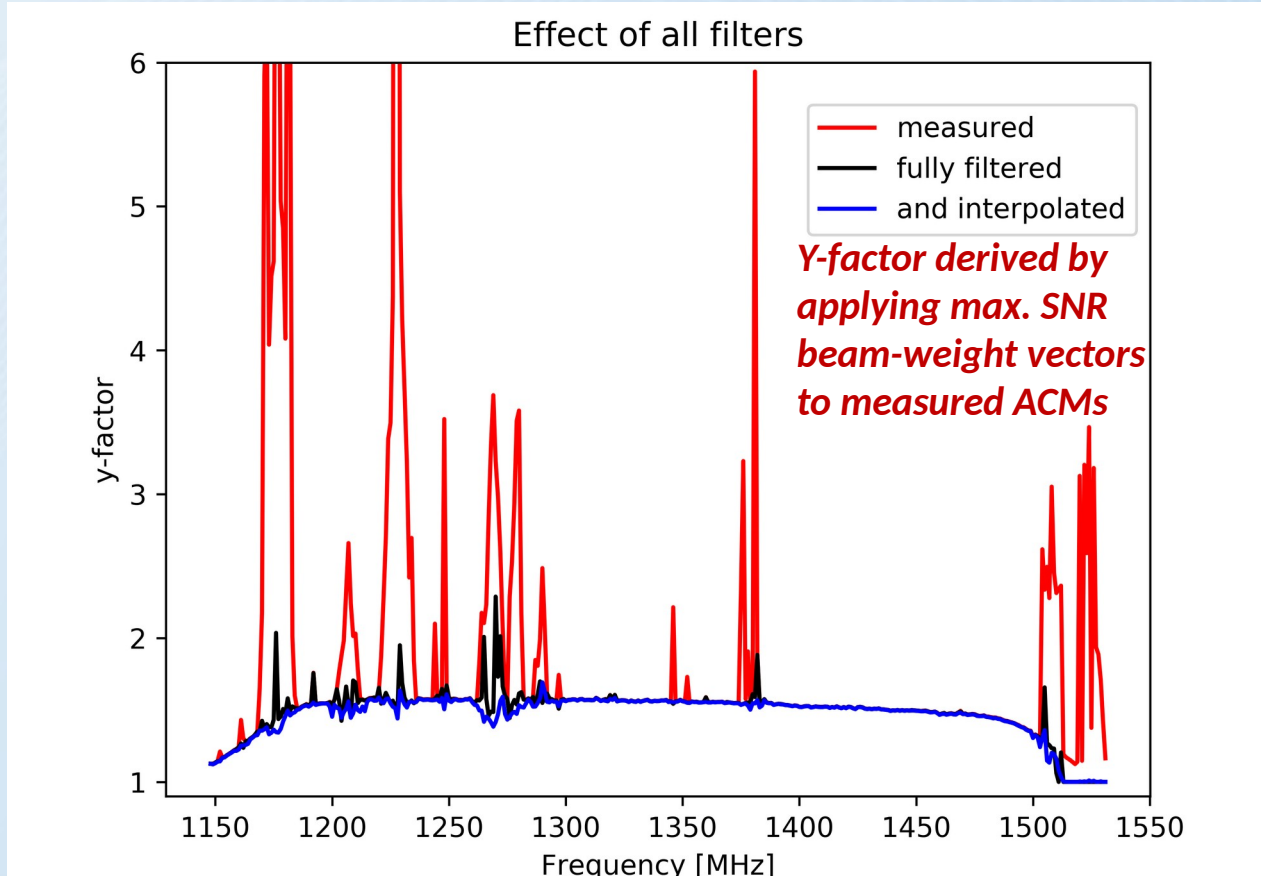
→interpolation can cause problems



RFI mitigation algorithms (3)



- Combining the intensity and spacial filtering is possible
 - (1) intensity filtering of R_{on} and R_{off}
 - (2) using eigenvector selection on resulting $R_{\text{on}} R_{\text{off}}^{-1}$
 - (3) interpolate over still empty frequency ranges
- Is used in science operation (for FRB search) since June 2021





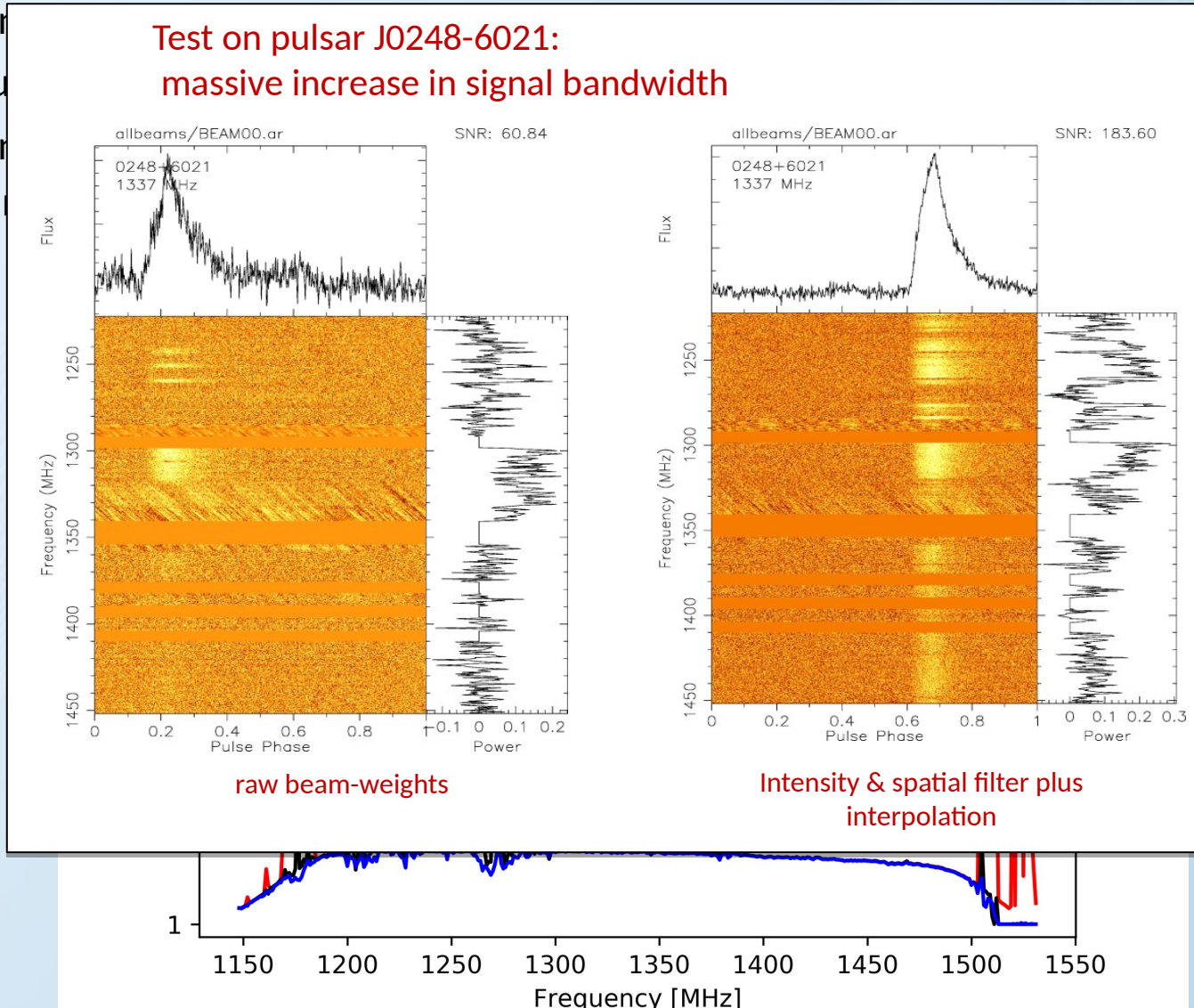
RFI mitigation algorithms (3)



- Combining the intensity and spacial filtering is possible

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RFI mitigation algorithms (4)



- Poor mans version for “static” RFI mitigation
 - RFI is usually not stable over time
 - ✓ WiFi signals or mobile phone signals have varying frequencies
 - ✓ telescope tracking changes directions all time
 - but observatory made RFI is often stable (CPU clock, LO-signal)
 - summing up many ACMs will result in better beam-weights

→this is a poor mans “filtering” over time of the signals
→takes a lot of time
→comes for free if relative amplitudes and phases between elements are maintained



RFI mitigation algorithms (4)



- Poor r

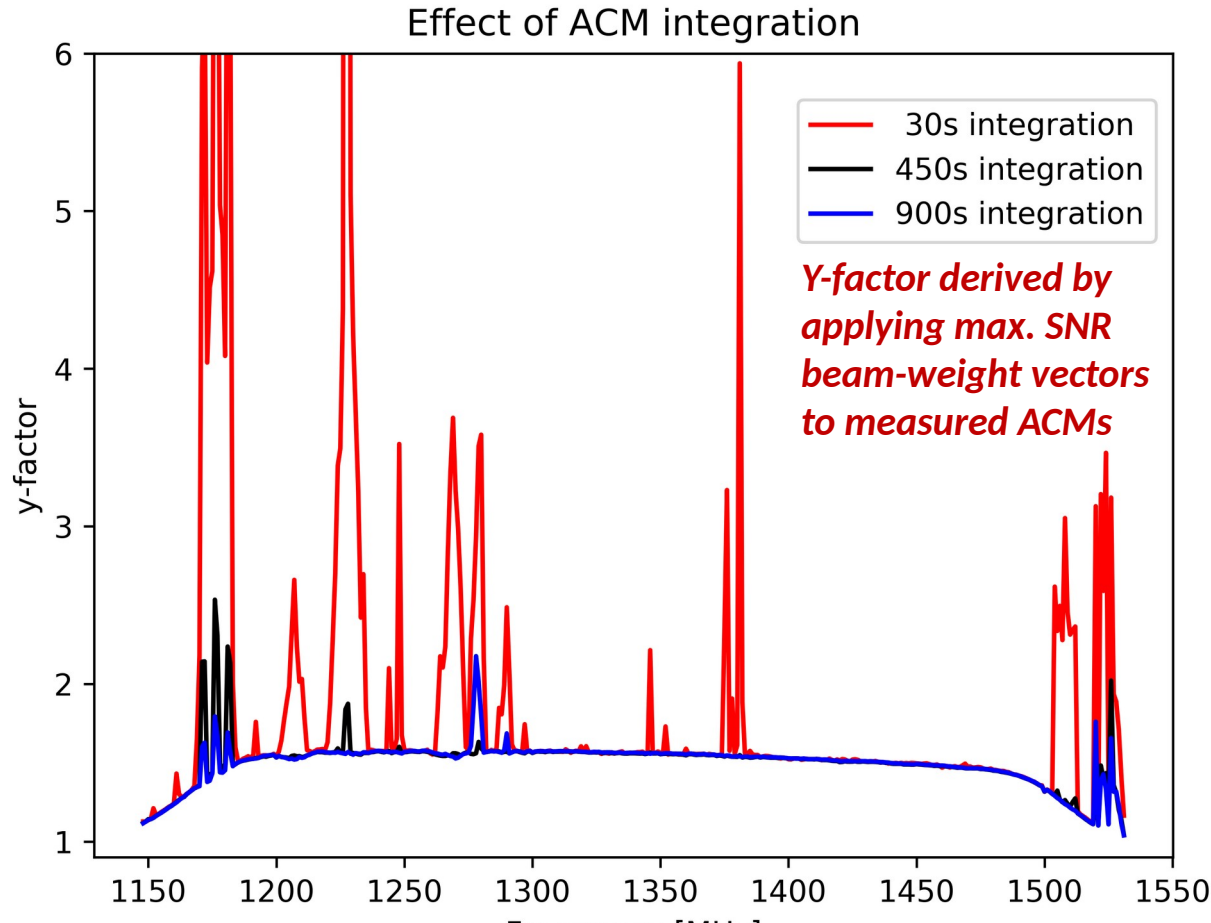
- RFI

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RFI mitigation algorithms (5)



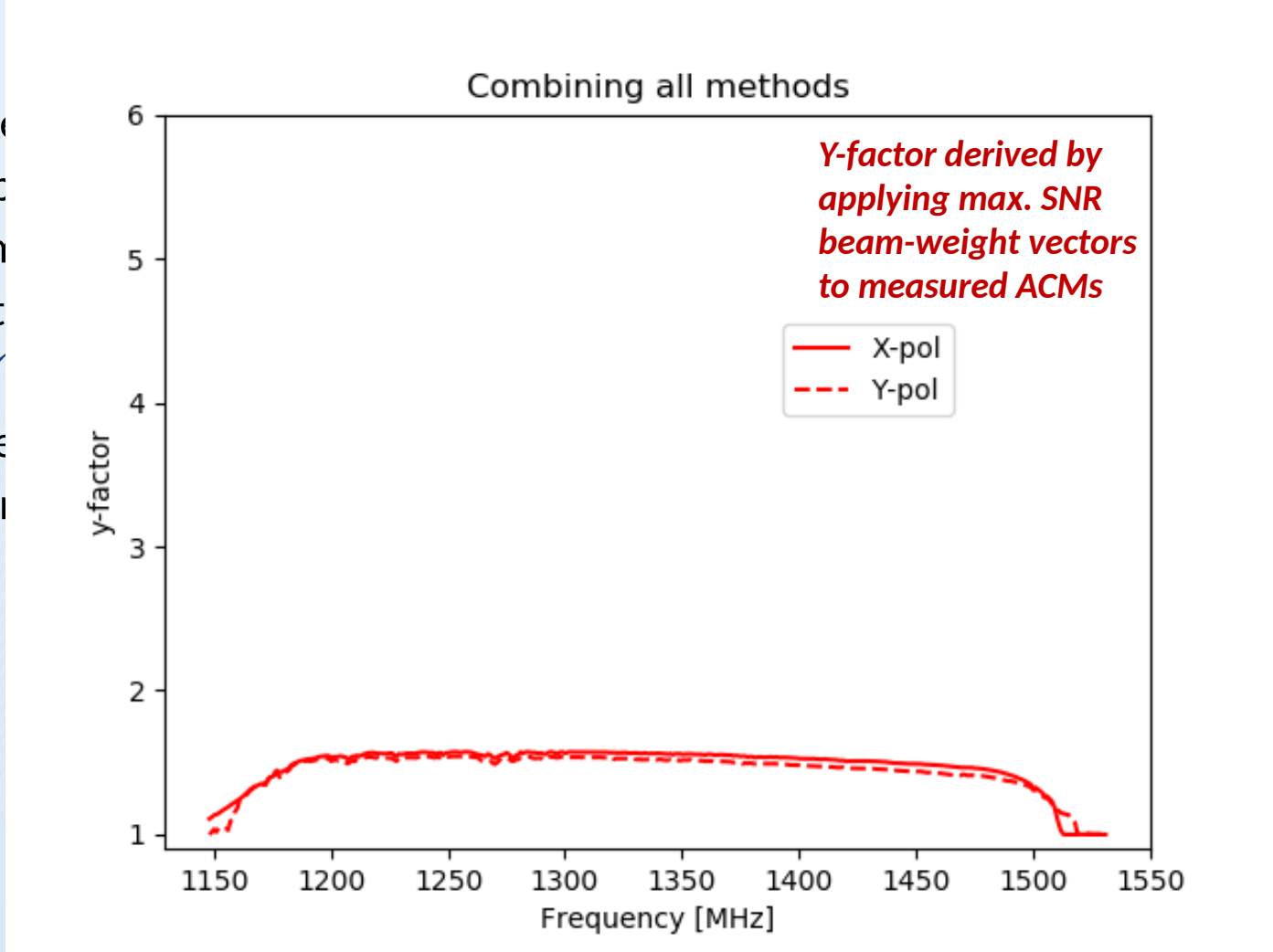
- Combine all the methods
 - take several (here 30) individual ACMs
 - apply intensity filter to each individual on and off ACM
 - sum up all on and all off source ACMs
 - determine solution space of $\mathbf{R}_{\text{on}}\mathbf{R}_{\text{off}}^{-1}$
 - ✓ select correct eigenvector (apply spacial filter)
 - interpolate over still empty areas
- scan over time deliver fully undisturbed reference beam-weights (steering vector)



RFI mitigation algorithms (5)



- Combining all methods
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 - app
 - sum
 - det
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Next steps

- “Static” RFI mitigation for beam-weight determination works
- within the cryoPAF we will have the capability to control the relative amplitudes and phases of all elements using our calibration unit
 - a beam-weight database is in planing
 - allowing for increasing accuracy of the beam-weights over time
- development of an online RFI mitigation is ongoing
 - projection of existing beam-weights to clean solution sub-space is required
 - main problem is to keep science data calibration fix
 - ✓ we will have a changing overall beam-efficiency
 - ✗ this can be calculated and therewith being removed
 - ✓ we will have a changing beam-pattern on sky
 - ✗ effect on main beam is small as long as efficiency change is small
 - ✗ but side-lobes will change
 - can have effects on (e.g. spectroscopic) mapping projects

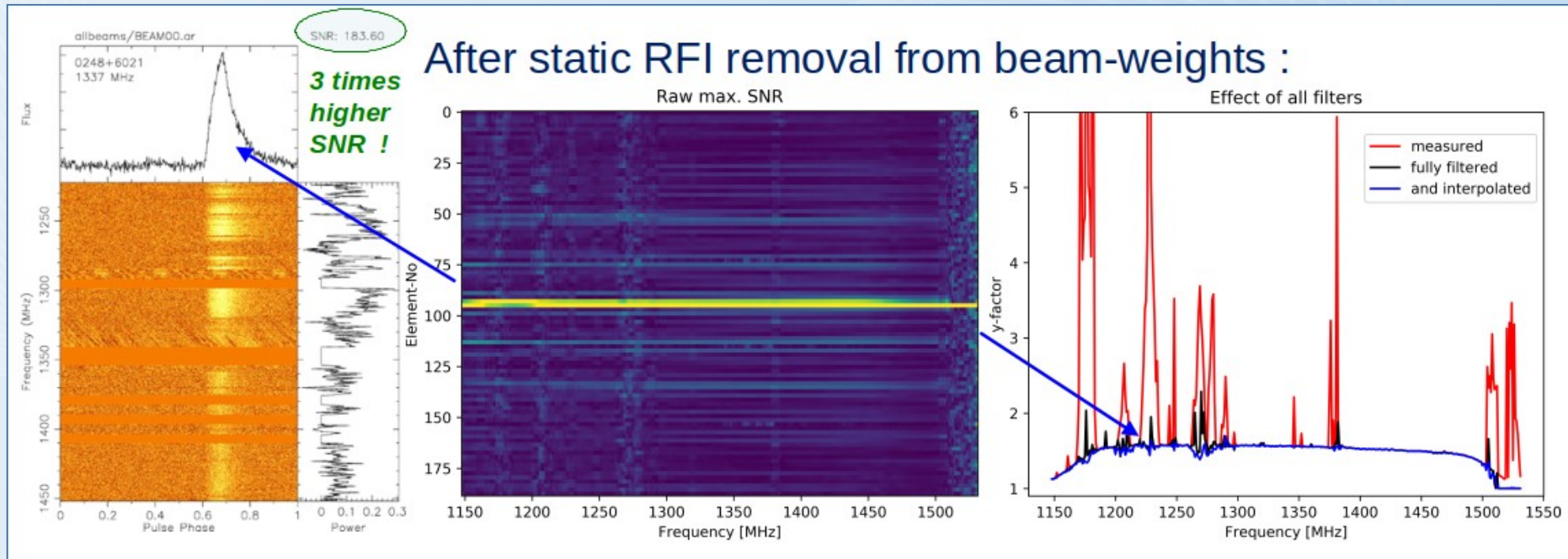
→ we will need time to make our experiences with this new technology



Conclusion



- “Static” RFI mitigation during beam-weight determination works reliably



- for the first generation cryo-PAF for the Effelsberg 100 m
 - we are foreseeing all necessary hardware to perform online RFI mitigation
- development of online RFI mitigation is ongoing
 - the new hardware is required for testing
 - time to make experience and adjust system to science cases is required